Decompose a graph into two disjoint cycles

高欣欣 中原大學

Consider a simple and undirected graph G. A set of subgraphs of G is disjoint if no two of them share a common vertex in G. Let |G| = n be the total number of vertices in G. For i = 1, 2, let n_i be an integer with $n_i \ge 3$, and $n_1 + n_2 = n$. Let $e(\overline{G})$ be the number of edges in the complement of G. We prove that if $e(\overline{G}) \le n-3$, then G contains two disjoint cycles with lengths n_1 and n_2 . The bound n-3 is sharp.